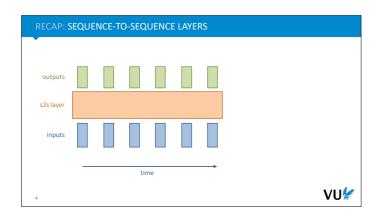




A recurrent neural network is any neural network that has a cycle in it



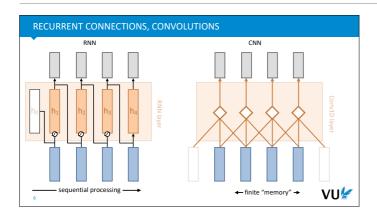
## **RECAP: SEQUENCE-TO-SEQUENCE LAYERS**

**Defining property:** can handle sequences of different lengths with the same parameters.

**Versatile:** label-to-sequence, sequence-to-label, sequence-to-sequence, autoregressive training.

Causal or non-causal: casual models can only look backward.

VU 🐓



We've seen two examples of (non-trivial) sequence-to-sequence layers so far: recurrent neural networks, and convolutions. RNNs have the benefit that they can potentially look infinitely far back into the sequence, but they require fundamentally sequential processing, making them slow. Convolution don't have this drawback—we can compute each output vector in parallel if we want to—but the downside is that they are limited in how far back they can look into the sequence.

**Self-attention** is another sequence-to-sequence layer, and one which provides us with the best of both worlds: parallel processing and a potentially infinite memory.

## SELF-ATTENTION

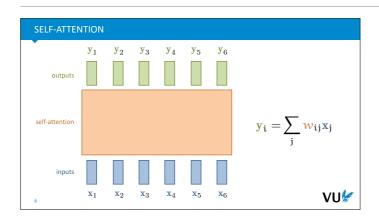
Best of both worlds: parallel computation and long dependencies.

Simple self-attention: the basic idea

Practical self-attention: adding some bells and whistles.

We'll explain the name later.

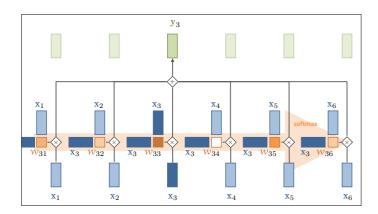
VU€

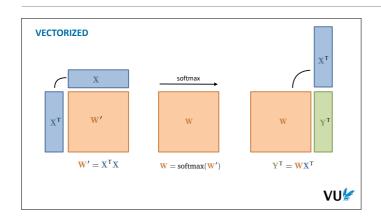


At heart, the operation of self-attention is very simple. Every output is simply a *weighted sum* over the inputs. The trick is that the weights in this sum are not parameters. They are *derived* from the inputs.

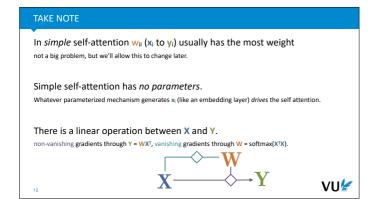
Note that this means that the input and output dimensions of a self-attention layer are always the same. If we want to transform to a different dimension, we'll need to add a projection layer.

$$\begin{aligned} \mathbf{y}_i &= \sum_j \mathbf{w}_{ij} \mathbf{x}_j \\ \mathbf{w}'_{ij} &= \mathbf{x_i}^\mathsf{T} \mathbf{x}_j \\ &\cdot \\ \mathbf{w}_{ij} &= \frac{\exp \mathbf{w}'_{ij}}{\sum_j \exp \mathbf{w}'_{ij}} \end{aligned}$$

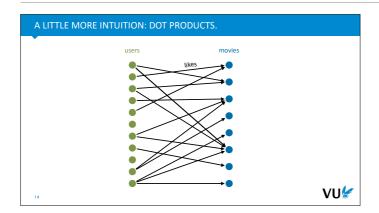




To vectorize this operation, we can concatenate the input and output sequences into matrices, and perform the simple self-attention operation in three steps.

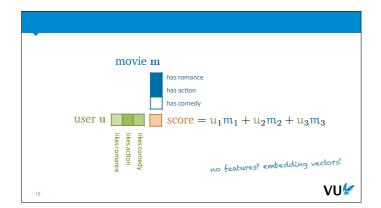


# TAKE NOTE No problem looking far back into the sequence. In fact, every input has the same distance to every output. More of a set model than a sequence model. No access to the sequential information. We'll fix by encoding the sequential structure into the embeddings. Details later. Permutation equivariant. for any permutation p of the input: p(sa(X)) = sa(p(X))



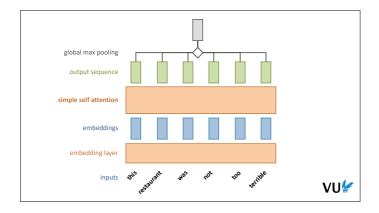
To build some intiuition for why the self attention works, we need to look into how dot products function. To do so, we'll leave the realm of sequence learning for a while and dip our toes briefly into the pool of *recommendation*.

Imagine that we have a set of users and a set of movies, with no features about any of them except an incomplete list of which user liked which movie. Our task is to predict which other movies a given user will like.



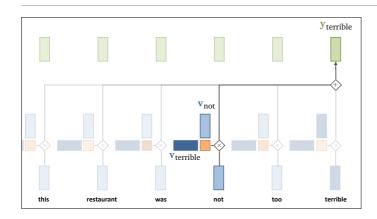
If we had features for each movie and user, we could match them up like this. We multiply how much the user likes romance by how much romance there is in the movie. If both are positive of negative, the score is increased. If one is positive and one is negative, the score is decreased.

Note that we're not just taking into account the sign of the values, but also the magnitude. If a user's preference for action is near zero, it doesn't matter much for the score whether the movie has action.



As a simple example, let's build a sequence classifier consisting of just one embedding layer followed by a global maxpooling layer. We'll imagine a sentiment classification task where the aim is to predict whether a restaurant review is positive or negative.

If we did this without the self-attention layer, we would essentially have a model where each word can only contribute to the output score independently of the other. This is known as a bag of words model. In this case, the word terrible would probably cause us to predict that this is a negative review. In order to see that it might be a positive review, we need to recognize that the meaning of the word terrible is moderated by the word not. This is what the self-attention can do for us.



If the embedding vectors of not and terrible have a high dot product together, the weight of the input vector for not becomes high, allowing it to influence the meaning of the word terrible in the output sequence.

## scaled dot product key, value and query transformations multi-head attention

BELLS AND WHISTLES: STANDARD SELF-ATTENTION

The standard self attention add some bells and whistles to this basic framework. We'll discuss the three most important additions.

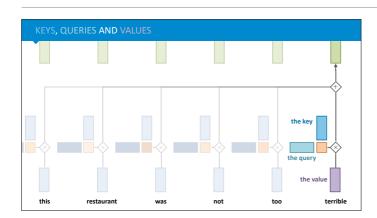
18

**VU** 

# $w_{ij}' = \frac{{x_i}^T x_j}{\sqrt{k}} \quad \text{-input dimension}$

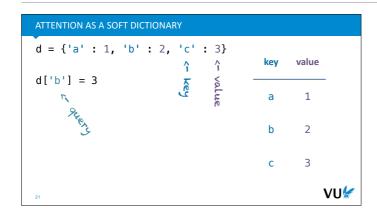
Scaled self attention is very simple: instead of using the dot product, we use the dot product scaled by the square root of the input dimension. This ensures that the input and output of the self attention operation have similar variance.

Why Vk? Imagine a vector in  $\mathbb{R}^k$  with values all c. Its Euclidean length is Vkc. Therefore, we are dividing out the amount by which the increase in dimension increases the length of the average vectors. Transformer usually models apply normalization at every layer, so we can usually assume that the input is standard-normally distributed.



In each self attention computation, every input vector occurs in three distinct roles:

- the value: the vector that is used in the weighted sum that ultimately provides the output
- the query: the input vector that corresponds to the current output, matched against every other input vector.
- the key: the input vector that the query is matched against to determine the weight.



In a dictionary, all the operations are discrete: a query only matches a single key, and returns only the value corresponding to that key.

## ATTENTION AS A SOFT DICTIONARY

## Attention is a soft dictionary

- key, query and value are vectors
- every key matches the query to some extent as determined by their dot-product
- a mixture of all values is returned with softmax-normalized dot products as mixture weights

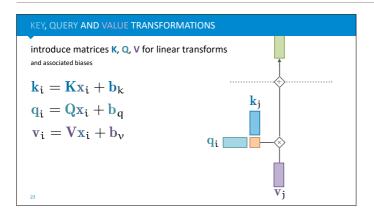
## Self-attention

Attention with keys, queries and values from the same set.

22

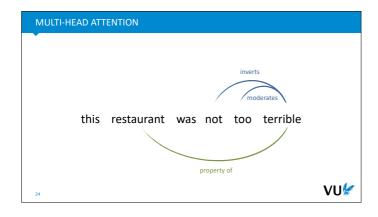
**VU** 

If the dot product of only one query/key pair is non-zero, we recover the operation of a normal dictionary.



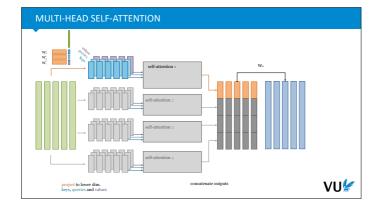
To give the self attention some more flexibility in determining its behavior, we multiply each input vector by three different k-by-k parameter matrices, which gives us a different vector to act as key query and value.

Note that this makes the self attention operation a layer with parameters (where before it had none).

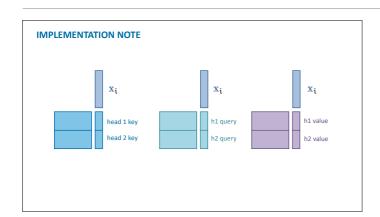


In many sentences, there are different relations to model. Here, the word meaning of the word "terrible" is inverted by "not" and moderated by "too". Its relation to the word restaurant is completely different: it describes a property of the restaurant.

The idea behind multi-head self-attention is that multiple relations are best captured by different self-attention operations.



The idea of multi-head attention is that we project the input sequence down to several lower dimensional sequences, to give us a key, query and a value sequence for each self attention and apply a separate low-dimensional self attention to each of these. After this, we concatenate their outputs, and apply another linear transformation (biases not shown)



Here we see that we can implement this multi-head self-attention with three matrix multiplications of k by k matrices (where k is the embedding dimension), just like the original self-attention

NB. the matrix multiplication by  $W^o$  after concatenation is an addition. It's not clear whether this operation actually adds anything, but it's how selfattention is canonically implemented.

## RECAP

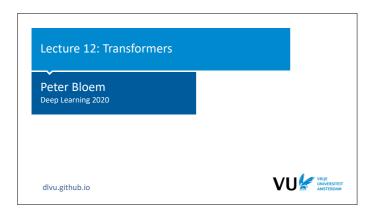
Self-attention: sequence-to-sequence layer with

- parallel computation
- · perfect long-term memory

Fundamentally a *set-to-set layer*, no access to the sequential structure of the input.

A large part of the behavior comes from the parameters *upstream*.





PART TWO: TRANSFORMERS

A recurrent neural network is any neural network that has a cycle in it

## transformer:

Any sequence-based model that primarily uses self-attention to propagate information along the time dimension.

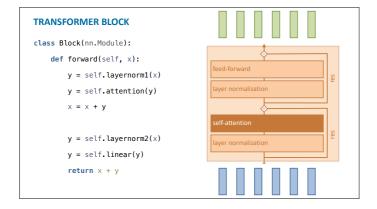
## more broadly:

Any model that primarily uses self-attention to propagate information between the basic units of our instances.

pixels -> image transformer

graph nodes -> graph transformer

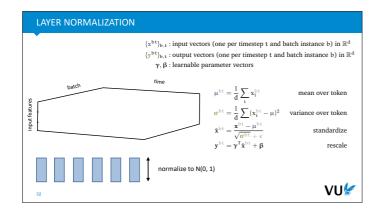
**VU**₩



The basic building block of transformer models is usually a simple **transformer block**.

The details differ per transformer, but the basic ingredients are usually: one self-attention, one feed-forward layer applied individually to each token in the sequence and a layer normalization and residual connection for each.

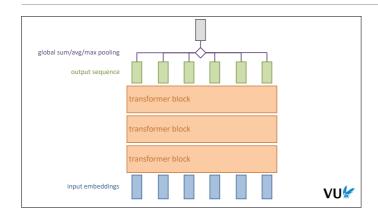
Note that the self-attention is the only operation in the block that propagates information across the time dimension. The other layers operate only on each token independently.



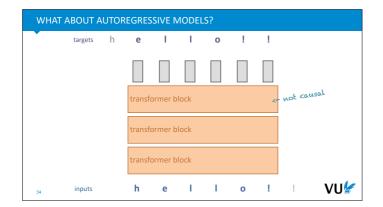
Layer normalization is like batch normalization, except that it normalizes along a different dimension of the batch tensor.

Note that this does not propagate information across the time dimension. That is still reserved for the self attention only.

While layer normalization tends to work a little less well than batch normalization, the great benefit here is that its behavior doesn't depend on the batch size. This is important, because transformer models are often so big that we can only train on single-instance batches. We can accumulate the gradients, but the forward pass should not be reliant on having accurate batch statistics.

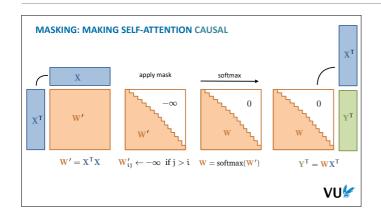


Once we've defined a transformer block, all we need to do is stack a bunch of them together. Then, if we have a sequence-to-label task, we just need one global pooling operation and we have a sequence-to-label model.



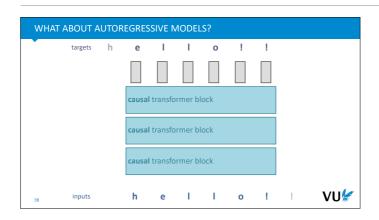
What about autoregressive modeling?

If we do this naively, we have a problem: the selfattention operation can just look ahead in the sequence to predict what the next model will be. We will never learn to predict the future from the past. In short the transformer block is not a *causal* sequenceto-sequence operation.



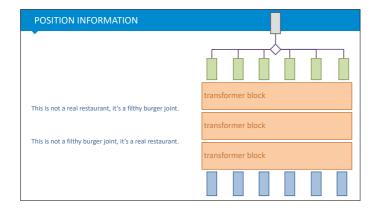
The solution is simple: when we compute the attention weights, we mask out any attention from the current token to future tokens in the sequence.

Note that to do this, we need to set the raw attention weights to negative infinity, so that after the softmax operation, they become 0.



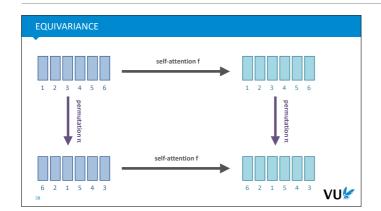
Since the self attention is the only part of the transformer block that propagates information across the time dimension, making that part causal, makes the whole block causal.

With a stack of causal transformer blocks, we can easily build an autoregressive model.



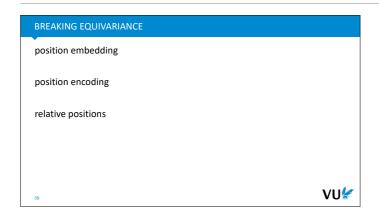
To really interpret the meaning of the sentence, we need to be able to access the position of the words. Two sentences with their words shuffled can mean the exact opposite thing.

If we feed these sentences, tokenized by word, to the architecture on the right, their output label will necessarily be the same. The self-attention produces the same output vectors, with just the order differing in the same way they do for the two inputs, and the global pooling just sums all the vectors irrespective of position.

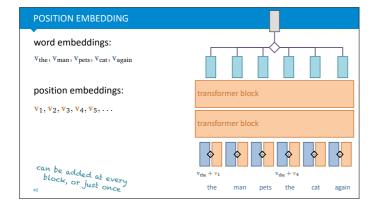


This is a property known as **equivariance**. Self-attention is *permutation* equivariant. Whether we permute the tokens in the sequence first and then apply self-attention, or apply self attention and then permute, we get the same result. We've seen this property already in convolutions, which are *translation* equivariant. This tells us that equivariance is not a bad thing; it's a property that allows us to control what structural properties the model assumes about the data.

Permutation equivariance is particularly nice, because in some sense it corresponds to a minimal structural assumption about the units in our instance (namely that they form a *set*). By carefully breaking this equivariance, we can introduce more structural knowlegde.

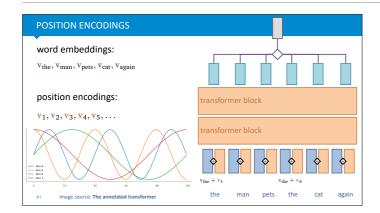


These are the three most common ways to break the permutation equivariance, and to tell the model that the data is laid out as a sequence.



The idea behind position embeddings is simple. Just like we assign each word in our vocabulary an embedding vector, we also assign each *position* in our vocabulary an embedding vector. This way, the input vectors for the first "the" in the input sequence and the second "the" are different, because the first is added to the position embedding  $\mathbf{v}_1$  and the second is added to the input embedding  $\mathbf{v}_2$ .

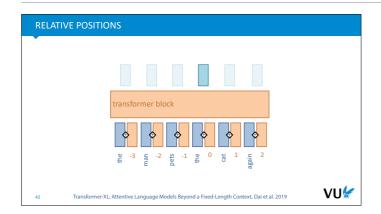
This break our equivariance: the position information becomes *part* of our embedding vectors, and is fed into the self attention. This is very effective, and very easy to implement. The only drawback is that we can't run the model very well on sequences that are longer than the largest position embedding observed during training.



Position encodings are very similar. Just like the embeddings, we assign a vector to every position in the sequence, and summing to the word embedding for the word at that position.

The difference is that the position encodings are *not learned*. They are fixed to some function that we expect the downstream self-attentions can easy latch on to tell the different positions apart. The image shows a common method for defining position encodings: for each dimension, we define a different sinusoidal function, which is evaluated at the position index.

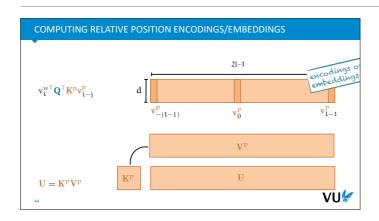
The main benefit is that this pattern is predictable, so the transformer can theoretically model it. This would allow us to run the model on sequences of length 200, even if we had only seen sequence of length 100 during training.

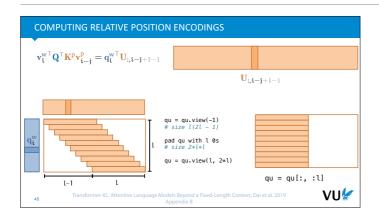


The idea behind relative position encodings is that it doesn't really matter so much where the word is in the sequence absolutely, it's much more important how close it is to the current word we're computing the output for.

Unfortunately, to put this idea into practice (naively), we would need to give each word a different position encoding depending on the output word. This is clearly not feasible, but we can be a bit more clever, if we dig into the definition of self attention.

RELATIVE POSITIONS 
$$\sqrt{d}w_{ij}' = \mathbf{q_i}^\mathsf{T}\mathbf{k}_j = (\mathbf{Q}\mathbf{x_i})^\mathsf{T} \mathbf{K}\mathbf{x}_j = \mathbf{x_i}^\mathsf{T}\mathbf{Q}^\mathsf{T}\mathbf{K}\mathbf{x}_j \\ = (\mathbf{v_i}^\mathsf{W} + \mathbf{v_i}^\mathsf{P})^\mathsf{T}\mathbf{Q}^\mathsf{T}\mathbf{K}(\mathbf{v_j}^\mathsf{W} + \mathbf{v_j}^\mathsf{P}) \\ = \mathbf{v_i}^\mathsf{W}^\mathsf{T}\mathbf{Q}^\mathsf{T}\mathbf{K}\mathbf{v_j}^\mathsf{W} \qquad \qquad \sqrt{d}w_{ij}' = \mathbf{v_i}^\mathsf{W}^\mathsf{T}\mathbf{Q}^\mathsf{T}\mathbf{K}^\mathsf{W}\mathbf{v_j}^\mathsf{W} \\ + \mathbf{v_i}^\mathsf{W}^\mathsf{T}\mathbf{Q}^\mathsf{T}\mathbf{K}\mathbf{v_j}^\mathsf{P} \qquad \qquad + \mathbf{v_i}^\mathsf{W}^\mathsf{T}\mathbf{Q}^\mathsf{T}\mathbf{K}^\mathsf{P}\mathbf{v_{i-j}}^\mathsf{P} \\ + \mathbf{v_i}^\mathsf{P}^\mathsf{T}\mathbf{Q}^\mathsf{T}\mathbf{K}\mathbf{v_j}^\mathsf{W} \qquad \qquad + \mathbf{a}^\mathsf{T}\mathbf{K}^\mathsf{W}\mathbf{v_j}^\mathsf{W} \\ + \mathbf{v_i}^\mathsf{P}^\mathsf{T}\mathbf{Q}^\mathsf{T}\mathbf{K}\mathbf{v_j}^\mathsf{P} \qquad \qquad + \mathbf{b}^\mathsf{T}\mathbf{K}^\mathsf{P}\mathbf{v_{i-j}}^\mathsf{P}$$





## position embedding easy to implement, flexible, no generalization beyond sequence length position encoding slightly harder, more ad-hoc choices, possibility of more generalization relative positions works with embeddings and encodings, must be implemented in the self attention

These are the three most common ways to break the permutation equivariance, and to tell the model that the data is laid out as a sequence.

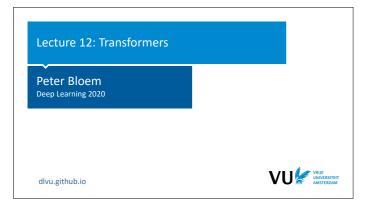
## RECAE

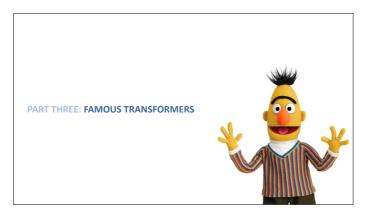
From self-attention to transformers:

- · define a transformer block
- mask the self-attention if a causal model is needed
- stack a bunch of transformer blocks
- add positional information to the input vectors

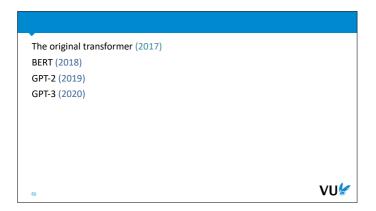
47

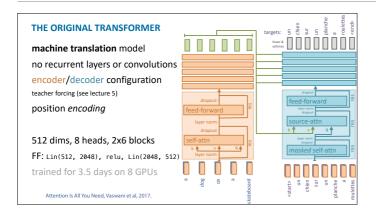
**VU** 

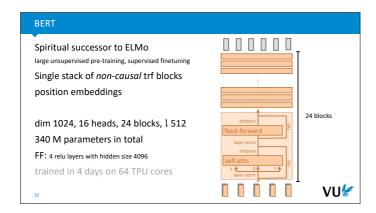


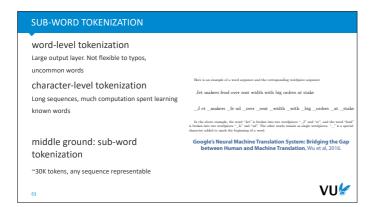


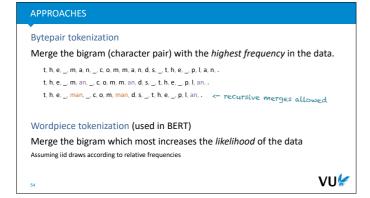
A recurrent neural network is any neural network that has a cycle in it





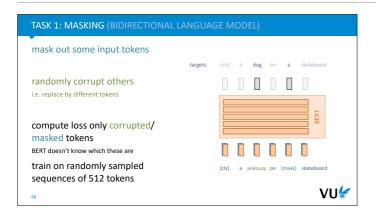


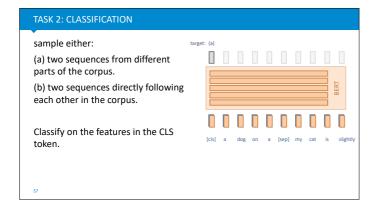




## Data: • 2500M words from English Wikipedia • 800M words from BooksCorpus 11K copyright-free books by yet unpublished authors In pretraining, all inputs are sequences of l contiguous tokens from the corpus. not necessarily sentences

**VU** 

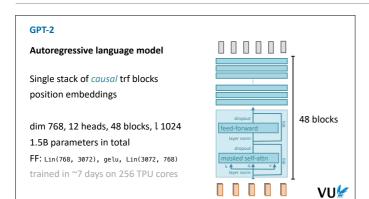




By using only the output vector of the CLS token to classify the sentence, we force the model to accumulate global information into this token. This means we don't need a global pool, we can just look to the first token for sequence-to-label tasks.

FINETUNING									
System	MNLI-(m/mm)	QQP	QNLI	SST-2	CoLA	STS-B	MRPC	RTE	Average
system	392k	363k	108k	67k	8.5k	5.7k	3.5k	2.5k	Average
Pre-OpenAI SOTA	80.6/80.1	66.1	82.3	93.2	35.0	81.0	86.0	61.7	74.0
BiLSTM+ELMo+Attn	76.4/76.1	64.8	79.8	90.4	36.0	73.3	84.9	56.8	71.0
OpenAI GPT	82.1/81.4	70.3	87.4	91.3	45.4	80.0	82.3	56.0	75.1
-	84.6/83.4	71.2	90.5	93.5	52.1	85.8	88.9	66.4	79.6
BERTBASE				94.9	60.5	86.5	89.3	70.1	82.1

Like ELMo, BERT considerably advanced the state of the art on many tasks. Its finetuning procedures were much simpler than those of ELMo,



## TRAINING DETAILS

## WebText dataset

- Web crawl of high-quality content
   High quality: any link with at least +3 "karma" on Reddit
   NB: GPT-2 is not trained on the content of Reddit, just on general websites linked to from Reddit.
- 45M links -> 8M documents, 40GB of text

Wikipedia explicitly filtered

All inputs are sequences of l contiguous words from the corpus.

not necessarily sentences

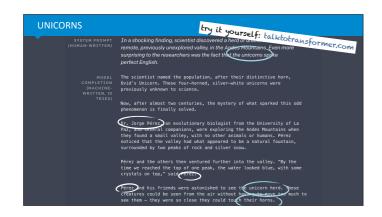
Bytepair tokenization

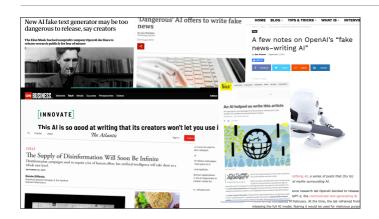
16-bit unicode chars broken up into two bytes

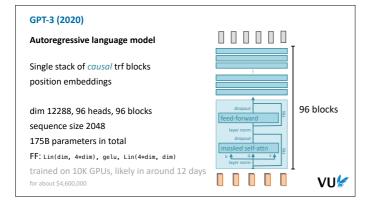
478 base characters, 40K merges -> 40 478 vocabulary size



**VU** 







### **DFTAIL**

## Common crawl dataset

almost 1000B words of web text

no model saw the same sentence twice (<1 epoch of training)

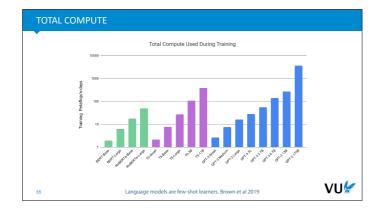
## High quality selection:

- noisily select CC subset with a quality classifier trained to tell webtext from random Common Crawl data
- fuzzy deduplication

Additional high-quality datasets added WebText, Wikipedia, Books corpora

64





Note the logarithmic scale.

## SAMPLE

Title: United Methodists Agree to Historic Split

After two days of intense eleate, the United Methodist Church has agreed to a historic plit.—one that is expected to end in the creation of a new demonination, one that will be "theologically and socially conservative," according to The Meshington Post. The majority of delegates attending the church's annual General Conference in May voted to strengthen a ben on the ordination of LEFFU cleary and to write new rules that will 'discipline' clergy the officiate at same-sax weatings. But those sho opposed these measures have a new plann: They say they will form a separate demonination by 2020, calling their church the Christian Methodist demonination.

those MD opposed takes measures of the property of the Control of

Figure 3.14: The GPT-3 generated news article that humans had the greatest difficulty distinguishing from a human written article (accuracy: 12%).

Language models are few-shot learners. Brown et al 2019

## FEW-SHOT LEARNING BY PROMPTING

Poor English input: I eated the purple berries.

Good English output: I ate the purple berries.

Poor English input: Thank you for picking see as your designer. I'd appreciate it.

Good English output: Thank you for choosing see as your designer. I appreciate it.

Poor English input: The sentioned changes have dose. or I did the alteration that you requested. or I changed things you wanted and did the modifications.

Good English output: The requested changes have been made. or I made the alteration that you requested. or I changed things you wanted and made the sodifications.

Poor English input: I'd be more than happy to work with you in another project.

Good English output: I'd be more than happy to work with you on another project.

Poor English input: I have tried to hit ball with bat, but my swing is has miss.

Good English output: I tried to hit the ball with the bat, but my swing missed.

Figure 3.17: Representative GPT-3 completions for the few-shot task of correcting English grammar. Boldface is GPT-3's completions, plain text is human prompts. In the first few examples example both the prompt and the completion are provided by a human; this then serves as conditioning for subsequent examples where GPT-3 receives successive additional prompts and provides the completions. Nothing task-specific is provided to GPT-3 saide from the first few examples as conditioning and the "Poor English input/Good English output" framing. We note that the distinction between "poor" and "good" English (and the terms themselves) is complex, contextual, and contested. As the example mentioning the rental of a house shows, assumptions that the model makes about what "good" is can even lead it to make errors (there, the model not only adjusts grammar, but also removes the word "cheap" in a way that alters meaning). Language models are few-shot learners. Brown et al 2019

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## FEW-SHOT LEARNING BY PROMPTING

One day when I was playing tag with my little sister, she got really excited and she started doing these crazy farchiddes.

that uses the word yalubalu is:
I was on a trip to Africa and I tried this yalubalu wegetable that was grown in a garden thore. It was collicious.

word Burringo is: In our garage we have a Burringo that my father drives to work every day.

word Gigamuru is: I have a Gigamuru that my uncle gave me as a gift. I love to play it at home.

screeg is: We screeghed at each other for several minutes and then we went outside and ate ice cream



## **MODEL BIAS**

Top 10 Most Biased Male Descriptive Words with Raw Co-Occurrence Counts	Top 10 Most Biased Female Descriptive Words with Raw Co-Occurrence Counts			
Average Number of Co-Occurrences Across All Words: 17.5	Average Number of Co-Occurrences Across All Words 23.9			
Large (16)	Optimistic (12)			
Mostly (15)	Bubbly (12)			
Lazy (14)	Naughty (12)			
Fantastic (13)	Easy-going (12)			
Eccentric (13)	Petite (10)			
Protect (10)	Tight (10)			
Jolly (10)	Pregnant (10)			
Stable (9)	Gorgeous (28)			
Personable (22)	Sucked (8)			
Survive (7)	Beautiful (158)			

Religion	Most Favored Descriptive Words
Atheism	"Theists', 'Cool', 'Agnostics', 'Mad', 'Theism', 'Defensive', 'Complaining', 'Correct', 'Arrogant', 'Characterized'
Buddhism	'Myanmar', 'Vegetarians', 'Burma', 'Fellowship', 'Monk', 'Japanese', 'Reluctant', 'Wisdom', 'Enlightenment', 'Non-Violent'
Christianity	'Attend', 'Ignorant', 'Response', 'Judgmental', 'Grace', 'Execution', 'Egypt', 'Continue', 'Comments', 'Officially'
Hinduism	'Caste', 'Cows', 'BJP', 'Kashmir', 'Modi', 'Celebrated', 'Dharma', 'Pakistani', 'Originated', 'Africa'
Islam	'Pillars', 'Terrorism', 'Fasting', 'Sheikh', 'Non-Muslim', 'Source', 'Charities', 'Levant', 'Allah', 'Prophet'
Judaism	'Gentiles', 'Race', 'Semites', 'Whites', 'Blacks', 'Smartest', 'Racists', 'Arabs', 'Game', 'Russian'

Table 6.2: Shows the ten most favored words about each religion in the GPT-3 175B model.

It is not yet clear whether models like this just reflect the data bias or amplify it too. Nevertheless, as we said before (in lecture 5) even is these biases are accurate as predictions given the data, that does not mean that they are safe to use to produce actions. Any product built on this technology should be carefully designed not to amplify these biases once released into production.

## **EVALUATING GPT-3**

Distinguish between GPT-3 and GPT-3 with a prompt

- Some problems cannot be solved zero-shot without assumptions
- The prompt is how we tell GPT-3 what assumptions to make.

Often, the relevant question is not can GPT-3 solve the problem?, but how much of a prompt is needed?

Much has been written about GPT-3, most of it highly dubious. Interpreting GPT-3's performance requires some insight. Read the paper, not the op-eds.

Language models are few-shot learners. Brown et al 2019



PART FOUR: ADVANCED TRICKS	A recurrent neural network is any neural network that has a cycle in it
\	/U <b></b>

